

$$\frac{7}{2} = \frac{7 \times 2}{2 \times 2} = \frac{14}{4}$$

$$\frac{5}{2} = \frac{5 \times 2}{2 \times 2} = \frac{10}{4}$$

$\therefore \frac{10}{4}$ and $\frac{14}{4}$ are less than $\frac{35}{4}$

\therefore both $\frac{7}{2}$ and $\frac{5}{2}$ are less than $\frac{35}{4}$

\therefore product of two improper fractions is greater than both the improper fractions.

82/783

6. Number \times Reciprocal of Number
 $=$ Number $\times \frac{1}{\text{Number}}$

$$= 1 \checkmark$$

7. Number > 1

$$\therefore \frac{\text{Number}}{\text{Number}} > \frac{1}{\text{Number}}$$

$$\therefore 1 > \text{Reciprocal of Number}$$

$$\therefore \text{Reciprocal of Number} < 1 \checkmark$$

8. Multiplicative inverse of $\frac{3}{5} = \frac{5}{3} = 1\frac{2}{3}$

$$9. \frac{15}{16} \times \text{---} = 1$$

$$\therefore \text{---} = 1 \div \frac{15}{16} = 1 \times \frac{16}{15} = \frac{16}{15} \checkmark$$

$$10. 1 \div \text{---} = 1\frac{2}{3}$$

$$\therefore 1 = 1\frac{2}{3} \times \text{---}$$

$$1 = \frac{5}{3} \times \text{---}$$

$$\therefore \text{---} = 1 \div \frac{5}{3} = 1 \times \frac{3}{5}$$

$$= \frac{3}{5} \checkmark$$

← X ←

$$\begin{aligned}
 &= \frac{\text{Novel}}{2} \\
 \text{b) part of Novel left to read} &= \text{Novel} - \frac{\text{Novel}}{2} \\
 &= \frac{2 \text{Novel} - \text{Novel}}{2} \\
 &= \frac{\text{Novel}}{2}
 \end{aligned}$$

But No. of pages left = 100 (given)

$$\therefore \frac{\text{Novel}}{2} = 100$$

$$\therefore \text{Novel} = 2 \times 100 = 200.$$

\therefore there are 200 pages in it

81/783

c) using ⁵⁴time increase her knowledge. she has reading habit.

MENTAL MATHS

$$\begin{aligned}
 1) \quad \frac{1}{2} + \frac{1}{3} - \frac{5}{6} \\
 &= \frac{(1 \times 3) + (1 \times 2) - 5}{6} \\
 &= \frac{3 + 2 - 5}{6} = \frac{5 - 5}{6} = 0
 \end{aligned}$$

$$2. \quad 2 \frac{3}{5} - 1 = \frac{13}{5} - 1 = \frac{13 - 5}{5} = \frac{8}{5} = 1 \frac{3}{5}$$

$$3. \quad \frac{1}{a} \times \frac{1}{b} = \frac{1 \times 1}{a \times b} = \frac{1}{ab} \checkmark$$

$$4. \quad \frac{1}{2} \text{ of } \frac{1}{y} = \frac{1}{2} \times \frac{1}{y} = \frac{1}{2y} \checkmark$$

$$5. \quad \frac{7}{2} \times \frac{5}{2} = \frac{7 \times 5}{2 \times 2} = \frac{35}{4}$$

$$\frac{7}{2} = \frac{7 \times 2}{2 \times 2} = \frac{14}{4}$$

$$\frac{5}{2} = \frac{5 \times 2}{2 \times 2} = \frac{10}{4}$$

$\therefore \frac{10}{4}$ and $\frac{14}{4}$ are less than $\frac{35}{4}$

\therefore both $\frac{7}{2}$ and $\frac{5}{2}$ are less than $\frac{35}{4}$

\therefore product of two improper fractions is greater than both the improper fractions.

$$\frac{1}{3} = \frac{1}{3} \times \frac{5}{5} = \frac{5}{15}$$

$$\frac{2}{5} = \frac{2}{5} \times \frac{3}{3} = \frac{6}{15}$$

$$\therefore \frac{6}{15} > \frac{5}{15} > \frac{4}{15}$$

$$\therefore \frac{2}{5} > \frac{1}{3} > \frac{4}{15}$$

\therefore maximum part of work done by Gautam. i.e. $\frac{2}{5}$.

d) Gautam and Manish show the nature of helping oth

80/783

53

2 (a) Novel read on 1st day = $\frac{1}{4} \times \text{Novel}$

Remaining part = $(1 - \frac{1}{4}) \times \text{Novel}$

= $\frac{3}{4} \times \text{Novel}$.

part of Novel read on 2nd day

= $\frac{1}{3}$ of $\frac{3}{4} \times \text{Novel}$

= $\frac{1}{3} \times \frac{3}{4} \times \text{Novel}$

= $\frac{1}{4} \times \text{Novel}$.

part of Novel read in 2 days.

= $\frac{\text{Novel}}{4} + \frac{\text{Novel}}{4}$

= $\frac{\text{Novel} + \text{Novel}}{4}$

= $\frac{2 \text{ Novel}}{4}$

= $\frac{\text{Novel}}{2}$

b) part of Novel left to read = $\text{Novel} - \frac{\text{Novel}}{2}$

= $\frac{2 \text{ Novel} - \text{Novel}}{2}$

= $\frac{\text{Novel}}{2}$.

But No. of pages left = 100 (given)

$\therefore \frac{\text{Novel}}{2} = 100$

$\therefore \text{Novel} = 2 \times 100 = 200$.

\therefore There are 200 pages in the book.

1. Reciprocal of 1 = $\frac{1}{1} = 1$

∴ Answer = (a) ✓

8. $1 \div \frac{2}{16} = 1 \times \frac{16}{2} = \frac{16}{2}$

∴ Answer = (b) ✓

9. $\frac{1}{2} \div 8 = \frac{1}{2} \times \frac{1}{8} = \frac{1}{16}$

∴ Answer = (c) ✓

10. $(5 \div \frac{3}{10}) \times \frac{9}{25} = (5 \times \frac{10}{3}) \times \frac{9}{25} = \frac{50}{3} \times \frac{9}{25} = \frac{2}{3} \times \frac{3}{1} = 2$

∴ Answer = (a) ✓

Value Based Questions.

↓ a) part of work done by Kishan and Gautam

$$= \frac{1}{3} + \frac{2}{5}$$

$$= \frac{(1 \times 5) + (2 \times 3)}{15}$$

$$= \frac{5 + 6}{15} = \frac{11}{15}$$

b) part of work done by Manish

$$= 1 - \frac{11}{15}$$

$$= \frac{(1 \times 15) - 11}{15} = \frac{15 - 11}{15}$$

$$= \frac{4}{15}$$

c) compare $\frac{1}{3}$, $\frac{2}{5}$, $\frac{4}{15}$

L.C.M of 3, 5 and 15 = 15

Common denominator = 15

$$\frac{1}{3} = \frac{1}{3} \times \frac{5}{5} = \frac{5}{15}$$

$$\frac{2}{5} = \frac{2}{5} \times \frac{3}{3} = \frac{6}{15}$$

$$\therefore \frac{6}{15} > \frac{5}{15} > \frac{4}{15}$$

$$\therefore \frac{2}{5} > \frac{1}{3} > \frac{4}{15}$$

∴ Maximum part of work done by Gautam, i.e. $\frac{2}{5}$.

d) Gautam and Manish show the nature of helping others in need

2. (a) Novel read on 1st day = $\frac{1}{4} \times \text{Novel}$

1. $\frac{1}{3}$ of 3 = $\frac{1}{3} \times 3 = 1$ \therefore Answer is (a) ✓

2. $\frac{1}{4}$ of $\frac{1}{4}$ = $\frac{1}{4} \times \frac{1}{4} = \frac{1}{16}$ \therefore Answer is (c) ✓

3. $\frac{8}{27} \times \frac{9}{16} = \frac{1}{3 \times 2} = \frac{1}{6}$ \therefore Answer is (c) ✓

4. $\frac{5}{7}$ of Number = 300

$\therefore \frac{5}{7} \times \text{Number} = 300$

Number = $300 \div \frac{5}{7}$
 $= 300 \times \frac{7}{5}$
 $= 420$

\therefore Answer is (b) ✓

5. 1 period = $\frac{5}{6}$ hour.

\therefore 6 periods = $6 \times \frac{5}{6}$ hours.
 $= 5$ hours.

Answer is (a) ✓

6. Reciprocal of $\frac{5}{4} \times \frac{8}{15} =$

$= \frac{4 \times 15}{5 \times 8} = \frac{3}{2}$

\therefore Answer = (c)

7. Reciprocal of 1 = $\frac{1}{1} = 1$

\therefore Answer = (a) ✓

8. $1 \div \frac{5}{16} = 1 \times \frac{16}{5} = \frac{16}{5}$

\therefore Answer = (b) ✓

9. $\frac{1}{2} \div 8 = \frac{1}{2} \times \frac{1}{8} = \frac{1}{16}$

\therefore Answer = (c) ✓

10. $(5 \div \frac{3}{10}) \times \frac{9}{25} = (5 \times \frac{10}{3}) \times \frac{9}{25} = \frac{50}{3} \times \frac{9}{25}$

\therefore Answer = (a) ✓

Value Based Questions.

↓
a) part of work done by Kishan and Gautam

after the sale
 portion given to his Son = $\frac{1}{2}$ of $\frac{1}{2} \times \text{Land}$
 $= \frac{1}{2} \times \frac{1}{2} \times \text{Land}$
 $= \frac{1}{4} \times \text{Land}$.

Balance Land with the man = $\frac{\text{Land}}{2} - \frac{\text{Land}}{4}$
 $= \frac{2\text{Land} - \text{Land}}{4}$
 $= \frac{\text{Land}}{4}$

77/783

Land given to daughter = $\frac{1}{3}$ of Balance Land.

$= \frac{1}{3} \times \frac{\text{Land}}{4}$
 $= \frac{\text{Land}}{12}$

Fraction of Land left with the man

$= \text{Balance} - \frac{\text{Land}}{12}$
 $= \frac{\text{Land}}{4} - \frac{\text{Land}}{12}$
 $= \frac{3\text{Land} - \text{Land}}{12}$
 $= \frac{2\text{Land}}{12}$
 $= \frac{1}{6} \text{ of Land.}$

\therefore Fraction of Land left with the man
 $= \frac{1}{6} \checkmark$

Multiple Choice questions

1. $\frac{1}{3}$ of 3 = $\frac{1}{3} \times 3 = 1 \therefore$ Ans is (a) \checkmark

2. $\frac{1}{4}$ of $\frac{1}{4}$ = $\frac{1}{4} \times \frac{1}{4} = \frac{1}{16} \therefore$ Answer is (c)

3. $\frac{8}{27} \times \frac{9}{16} = \frac{1}{3 \times 2} = \frac{1}{6} \therefore$ Answer is (c)

4. $\frac{5}{7}$ of Number = 300

20 m used for 1 cushion = $2 + \frac{1}{2} \text{ m} \div 25$

$$\begin{aligned} &= \frac{55 \text{ m} \div 25}{2} \\ &= \frac{11}{2} \times \frac{1}{25} \text{ m} \\ &= \frac{11}{10} \text{ m} \\ &= 1 \frac{1}{10} \text{ m} \checkmark \end{aligned}$$

6: Time required for reading 80 pages of book
 $= \frac{2}{3}$ of hour.

\therefore Time required for reading ¹ page 19
 $= \frac{2}{3} \text{ hours} \div 80$
 $= \frac{2}{3} \times \frac{1}{80} \text{ hour.}$
 $= \frac{1}{120} \text{ hour.}$

\therefore Time needed for reading 840 pages
 $= \frac{1}{120} \text{ hour} \times 840$
 $= \frac{1}{120} \times 840 \text{ hours.}$
 $= 7 \text{ hours.} \checkmark$

\therefore Shashank can complete reading the Book in 7 hours.

7.
Land Remaining with a man = $\frac{1}{2} \times \text{Land.}$
after the sale.

Portion given to his Son = $\frac{1}{2}$ of $\frac{1}{2} \times \text{Land}$
 $= \frac{1}{2} \times \frac{1}{2} \times \text{Land}$
 $= \frac{1}{4} \times \text{Land.}$

Balance Land with the man = $\frac{\text{Land}}{2} - \frac{\text{Land}}{4}$
 $= \frac{2\text{Land} - \text{Land}}{4}$
 $= \frac{\text{Land}}{4}$

$$= \frac{295}{2} \text{ m}$$

$$= 147\frac{1}{2} \text{ m. } \checkmark$$

5. (a) Total length of cloth weaver has = $82\frac{1}{2} \text{ m}$
 Cloth required for 1 curtain = $2\frac{3}{4} \text{ m}$.

75/783

$$\text{cloth used for curtains} = \frac{2}{3} \text{ of } 82\frac{1}{2} \text{ m}$$

$$= \frac{2}{3} \times \frac{165}{2} \text{ m}$$

$$= 55 \text{ m.}$$

$$\therefore \text{No. of curtains stitched} = 55 \text{ m} \div 2\frac{3}{4} \text{ m}$$

$$= 55 \text{ m} \div \frac{11}{4} \text{ m}$$

$$= 55 \times \frac{4}{11}$$

$$= 20 \checkmark$$

b) Remaining cloth = $82\frac{1}{2} \text{ m} - 55 \text{ m}$

$$= 27\frac{1}{2} \text{ m.}$$

No. of cushion covers stitched = 25

$$\therefore \text{cloth used for 1 cushion} = 27\frac{1}{2} \text{ m} \div 25$$

$$= \frac{55}{2} \text{ m} \div 25$$

$$= \frac{55}{2} \times \frac{1}{25}$$

$$= \frac{11}{10} \text{ m}$$

$$= 1\frac{1}{10} \text{ m } \checkmark$$

6. Time required for reading 80 pages of book

$$= \frac{2}{3} \text{ of hour.}$$

4. No. of Students = 50

No. of Girls = $\frac{3}{5} \times 50 = 30$

\therefore No. of Boys = $50 - 30 = 20$

Ribbon Brought by each girl = $2\frac{3}{4}$ m

\therefore Ribbon collected by all girls = $2\frac{3}{4} \times 30$

= $\frac{11}{4} \times 30$ m

= $\frac{11 \times 15}{2}$ m

= $\frac{165}{2}$ m

74/783

Ribbon brought by each boy = $3\frac{1}{4}$ m

\therefore Ribbon collected by all boys = $3\frac{1}{4} \times 20$

= $\frac{13}{4} \times 20$ m

= 65 m

\therefore Ribbon collected by all students

= $\frac{165}{2}$ m + 65 m

= $\frac{165 + (2 \times 65)}{2}$ m

= $\frac{165 + 130}{2}$ m

= $\frac{295}{2}$ m

= $147\frac{1}{2}$ m. ✓

5. (a) Total length of cloth weaver has = $82\frac{1}{2}$ m

cloth required for 1 curtain = $2\frac{3}{4}$ m.

cloth used for curtains = $\frac{2}{3}$ of $82\frac{1}{2}$ m

= $\frac{2}{3} \times \frac{165}{2}$ m

48

$$= \left(\frac{(27 \times 3) + (3 \times 2)}{12} \right) \div \left(\frac{55}{48} \right)$$

$$= \frac{81 + 62}{12} \times \frac{48}{55}$$

$$= \frac{143}{12} \times \frac{48}{55}$$

$$= \frac{13 \times 4}{1 \times 5} = \frac{52}{5}$$

$$= 10 \frac{2}{5} \checkmark$$

LCM

$$\frac{2}{4} \frac{1}{6}$$

$$\frac{2}{2} \frac{1}{3}$$

$$\frac{3}{1} \frac{1}{3}$$

11

∴ LCM of 4 and 6

$$= 2 \times 2 \times 3$$

$$= 12$$

3.

Number of stamps with Divya = 180

$$\text{Stamps given to Tara} = \frac{1}{5} \times 180 = 36$$

$$= 36$$

$$\text{Stamps given to Mala} = \frac{1}{3} \times 36 = 12$$

$$= 12 \checkmark$$

$$\text{Stamps left with Tara} = 36 - 12 = 24 \checkmark$$

$$\text{Stamps left with Divya} = 180 - 36$$

$$= 144 \checkmark$$

4. No. of Students = 50

$$\text{No. of Girls} = \frac{3}{5} \times 50 = 30$$

$$\therefore \text{No. of Boys} = 50 - 30 = 20$$

$$\text{Ribbon Brought by each girl} = 2 \frac{3}{4} \text{ m}$$

$$\therefore \text{Ribbon collected by all girls} = 2 \frac{3}{4} \text{ m} \times 30$$

$$= \frac{11}{4} \times 30 \text{ m}$$

$$= \frac{11 \times 15}{2} \text{ m}$$

$$= \frac{165}{2} \text{ m}$$

$$\text{Ribbon brought by each boy} = 3 \frac{1}{4} \text{ m}$$

$$\therefore \text{Ribbon collected by all boys} = 3 \frac{1}{4} \text{ m} \times 20$$

$$= \frac{13}{4} \times 20 \text{ m}$$

47

$$\begin{aligned}
 \text{viii, } \frac{8}{7} - \left[\frac{1}{5} \text{ of } 3\frac{4}{7} \right] \\
 = \frac{8}{7} - \left[\frac{1}{5} \times \frac{25}{7} \right] \\
 = \frac{8}{7} - \frac{5}{7} \\
 = \frac{3}{7}
 \end{aligned}$$

$$\begin{aligned}
 \text{ix, } \left(\frac{9}{29} \times \frac{1}{12} \right) \times \left(6 - \frac{1}{5} \right) \times \left(\frac{1}{4} \times \frac{1}{5} \right) \\
 = \frac{3 \cancel{9} \times 1}{29 \times \frac{4}{4}} \times \left(\frac{(6 \times 5) - 1}{5} \right) \times \frac{1}{20} \\
 = \frac{3}{29 \times 4} \times \left(\frac{30 - 1}{5} \right) \times \frac{1}{20} \\
 = \frac{3}{29 \times 4} \times \frac{29}{5} \times \frac{1}{20} \\
 = \frac{3 \times \cancel{29} \times 1}{\cancel{29} \times 4 \times 5 \times 20} \\
 = \frac{3}{20 \times 20} \\
 = \frac{3}{400} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{x, } \left(6\frac{3}{4} + 5\frac{1}{6} \right) \div \left(\frac{11}{12} \times 3\frac{3}{4} \times \frac{1}{3} \right) \\
 = \left(\frac{27}{4} + \frac{31}{6} \right) \div \left(\frac{11}{12} \times \frac{15}{4} \times \frac{1}{3} \right)
 \end{aligned}$$

$$= \left(\frac{(27 \times 3) + (31 \times 2)}{12} \right) \div \left(\frac{55}{48} \right) \quad \left| \begin{array}{l} \text{LCM} \\ \frac{2(4/6)}{2(2/3)} \end{array} \right. \quad \frac{46}{1}$$

$$\begin{aligned}
 &= \frac{22 \times 7}{3} - \frac{1}{5} \\
 &= \frac{154}{3} - \frac{1}{5} \\
 &= \frac{(154 \times 5) - (3 \times 1)}{15} \\
 &= \frac{770 - 3}{15} \\
 &= \frac{767}{15} \\
 &= 51 \frac{2}{15} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{v)} \quad \frac{13}{12} \times 4 \frac{4}{5} \div \frac{13}{25} & \qquad \qquad \qquad \frac{44}{44} \\
 &= \left(\frac{13}{12} \times \frac{24}{5} \right) \div \frac{13}{25} \\
 &= \frac{13 \times 2}{1} \times \frac{25}{13} \\
 &= 2 \times 5 \\
 &= 10 \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{vi)} \quad \left[5 \frac{1}{2} \times 10 \frac{1}{2} \right] \text{ of } \frac{16}{55} & \\
 &= \frac{11}{2} \times \frac{21}{2} \times \frac{16}{55} \\
 &= \frac{1 \times 21 \times 8}{2 \times 1 \times 5} \\
 &= \frac{21 \times 4}{5} = \frac{84}{5} = 16 \frac{4}{5} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{vii)} \quad \left[1 \frac{7}{5} \times 15 \frac{1}{5} \right] \text{ of } \left[\frac{2}{5} \div 4 \right] & \\
 &= \left[\frac{12}{5} \times \frac{76}{5} \right] \times \left[\frac{2}{5} \times \frac{1}{4} \right] \\
 &= \frac{12}{5} \times \frac{76}{5} \times \frac{1}{5} \times \frac{1}{2} \\
 &= \frac{6 \times 76}{5 \times 5 \times 5} \\
 &= \frac{456}{125} = 3 \frac{81}{125} \checkmark
 \end{aligned}$$

$$\text{viii)} \quad \frac{8}{7} - \left[\frac{1}{5} \text{ of } 3 \frac{4}{7} \right] \qquad \qquad \qquad \frac{45}{45}$$

$$\begin{aligned}
 \text{iii), } & \left[4\frac{1}{55} \times \frac{5}{34} \right] \div \left[\frac{7}{8} \times \frac{5}{12} \right] \\
 & = \left[\frac{221}{55} \times \frac{5}{34} \right] \div \left[\frac{7 \times 5}{8 \times 12} \right] \\
 & = \frac{221}{11 \times 34} \times \frac{8 \times 12}{7 \times 5} \\
 & = \frac{13}{11} \times \frac{8 \times 6}{7 \times 5} \\
 & = \frac{624}{385} = 1\frac{239}{385} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{iv), } & \left[9\frac{3}{7} \times 5\frac{4}{9} \right] - \left[1\frac{2}{3} \div 8\frac{1}{3} \right] \\
 & = \left[\frac{66}{7} \times \frac{49}{9} \right] - \left[\frac{5}{3} \div \frac{25}{3} \right] \\
 & = \frac{22 \times 7}{3} - \left[\frac{1}{5} \times \frac{25}{5} \right] \\
 & = \frac{22 \times 7}{3} - \frac{1}{5} \\
 & = \frac{154}{3} - \frac{1}{5} \\
 & = \frac{(154 \times 5) - (3 \times 1)}{15} \\
 & = \frac{770 - 3}{15} \\
 & = \frac{767}{15} \\
 & = 51\frac{2}{15} \checkmark
 \end{aligned}$$